

PHENIX Summer 2010 Collaboration Meeting, July 12

QCD: the next decade

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BROOKHAVEN
NATIONAL LABORATORY

Outline

- The beginnings

From atoms (V century B.C.) to quarks;
atoms, void and geometry

- The successes

Symmetry; QCD as the gauge theory of strong interactions;
asymptotic freedom; hard processes; strong color fields

- The challenges

Confinement; chiral symmetry breaking; extreme QCD:
temperature, density, energy; the spin; void and geometry

- The mission for the next decade

**From particles to fields: collective phenomena
as the essence of QCD; the measurements**

The beginnings

Everything consists of

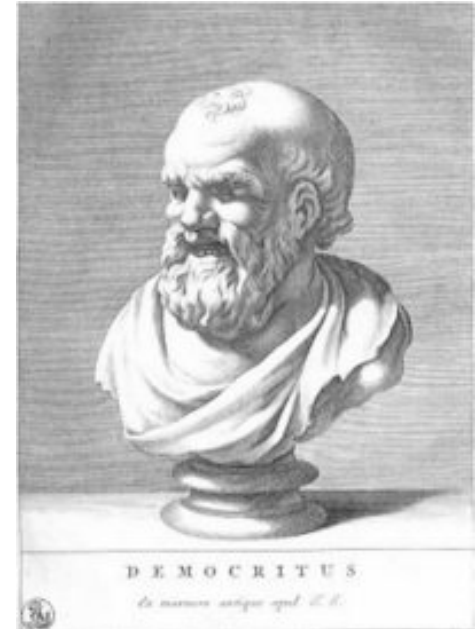
Atoms and Void

ἄτομος un - cuttable, indivisible

α- τέμνω



Λεύκιππος
Leucippus, V B.C.



Δημόκριτος
Democritus, ca 460 -370 B.C.

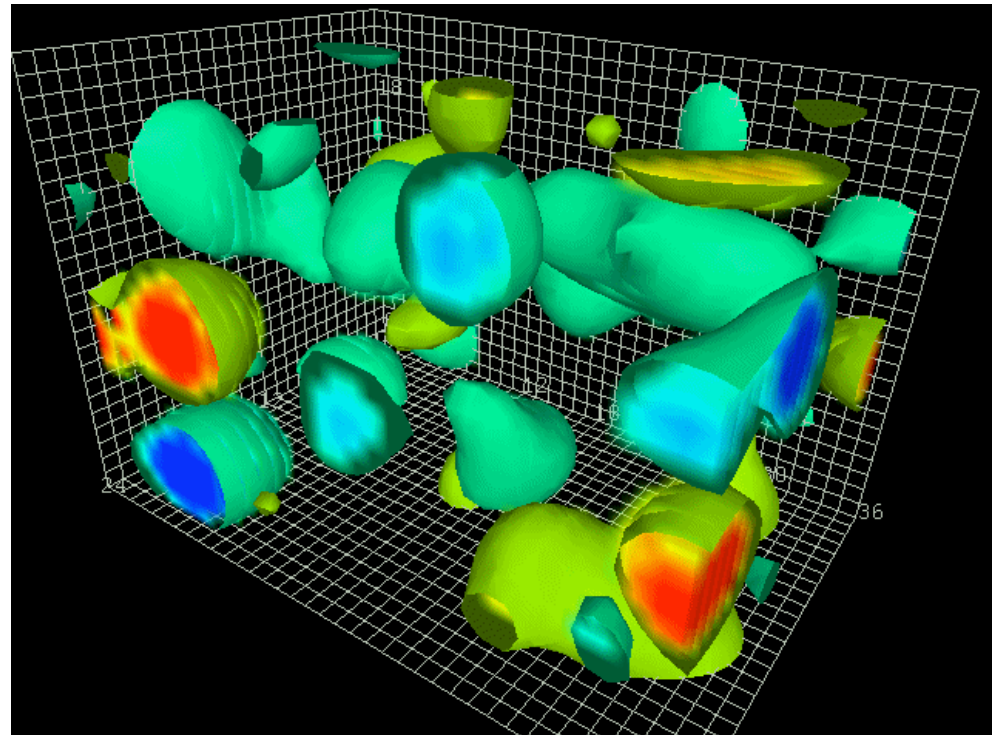
Everything consists of

Atoms and Void

“Atoms”,
ca 2010 A.D.

Void,
ca 2010 A.D.

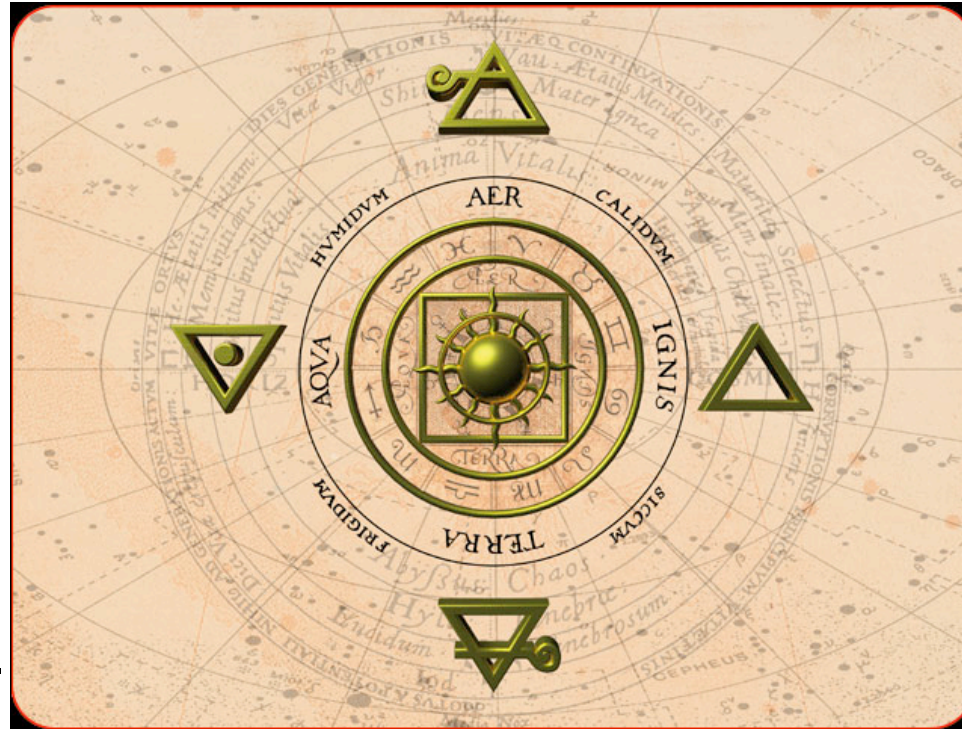
Leptons	Quarks		
	u up	c charm	t top
	d down	s strange	b bottom
	ν_e e- Neutrino	ν_μ μ - Neutrino	ν_τ τ - Neutrino
	e electron	μ muon	τ tau
	I	II	III
The Generations of Matter			



Atoms and Geometry, IV B.C.



Πλάτων
Plato, 428-348 B.C.



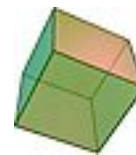
Fire



Air

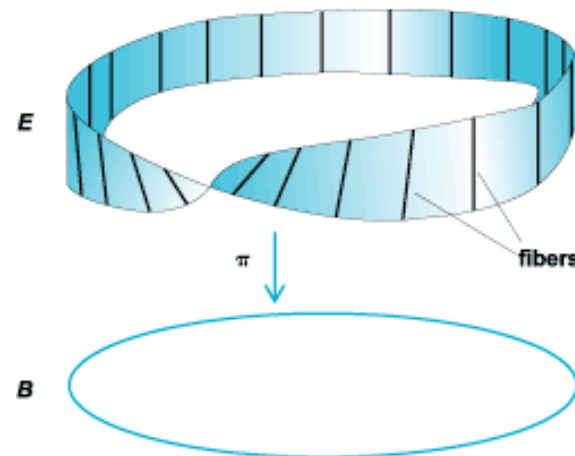
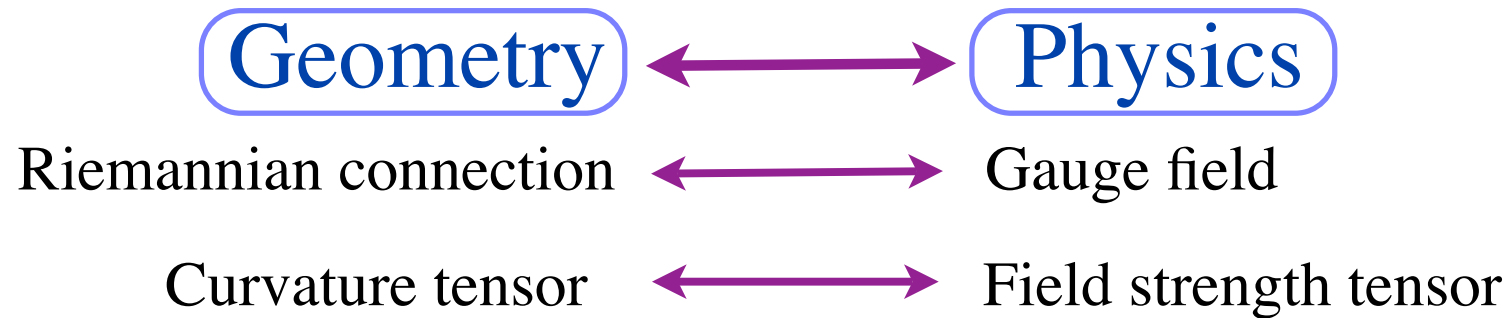


Water



Earth

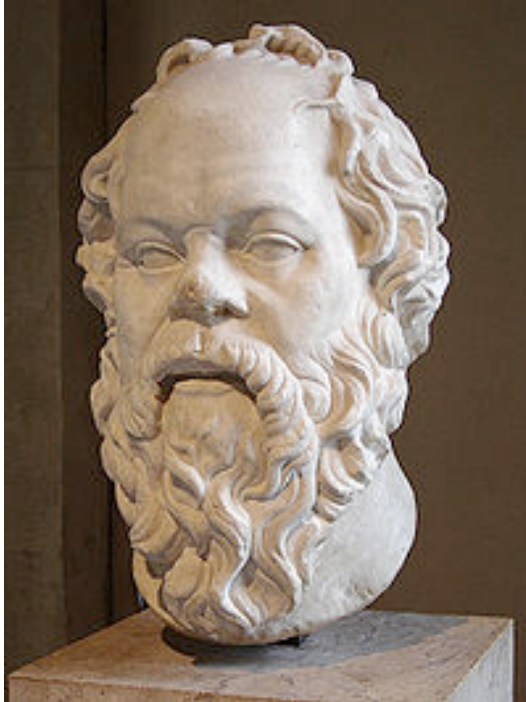
Atoms and Geometry, 2010 A.D.



Möbius strip, the simplest nontrivial example of a fiber bundle

Gauge theories “live” in a fiber bundle space that possesses non-trivial topology (knots, links, twists,...)

The metaphor of the cave, 380 B.C.



Socrates (Σωκράτης)
469 - 399 B.C.

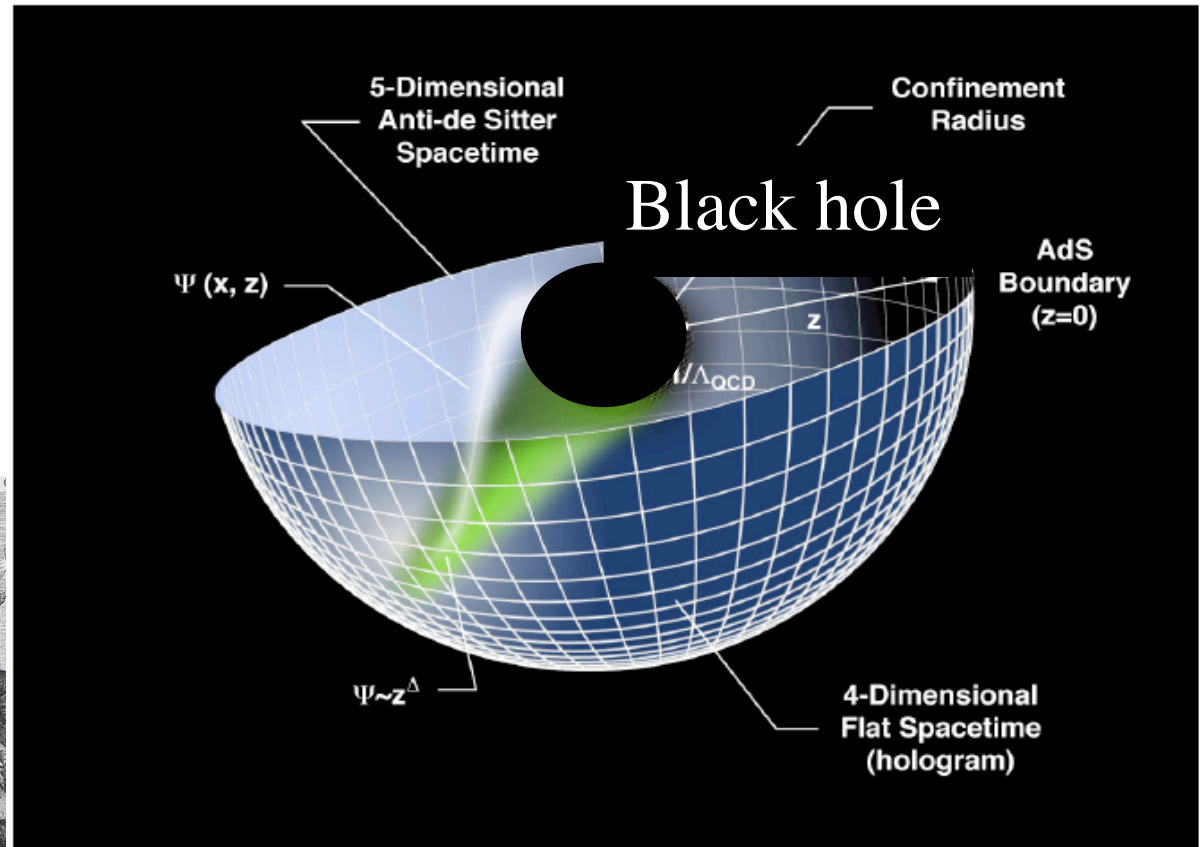
“Physical objects and physical events are only "shadows" of their ideal or perfect forms, and exist only to the extent that they instantiate the perfect versions of themselves”

Socrates, in Plato’s “Republic”



“The prisoners would take the shadows to be real things and the echoes to be real sounds, not just reflections of reality, since they are all they had ever seen or heard.”

The metaphor of the cave, 2010 A.D.



“The prisoners would take the shadows to be real things and the echoes to be real sounds, not just reflections of reality, since they are all they had ever seen or heard.”

The successes

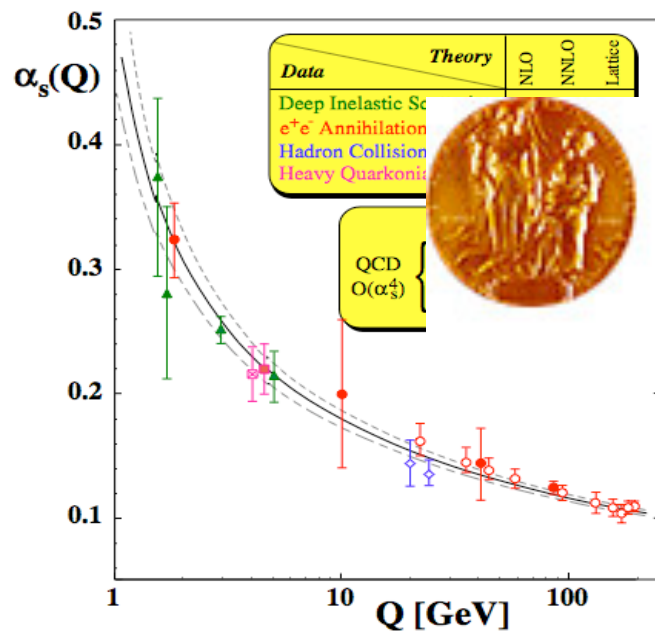
QCD = quarks + geometry

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{q}_f^a (i\gamma_\mu D_\mu - m_f) q_f^a;$$

$$D_\mu = \partial_\mu - igA_\mu^a t^a$$

Elegant, consistent, and correct theory

Asymptotic Freedom: “atoms” revealed



At short distances,
the strong force becomes weak
(**anti**-screening) -
one can access the “asymptotically
free” regime in hard processes

and in super-dense matter
(inter-particle distances $\sim 1/T$)

$$\alpha_s(Q) \simeq \frac{4\pi}{b \ln(Q^2/\Lambda^2)}$$

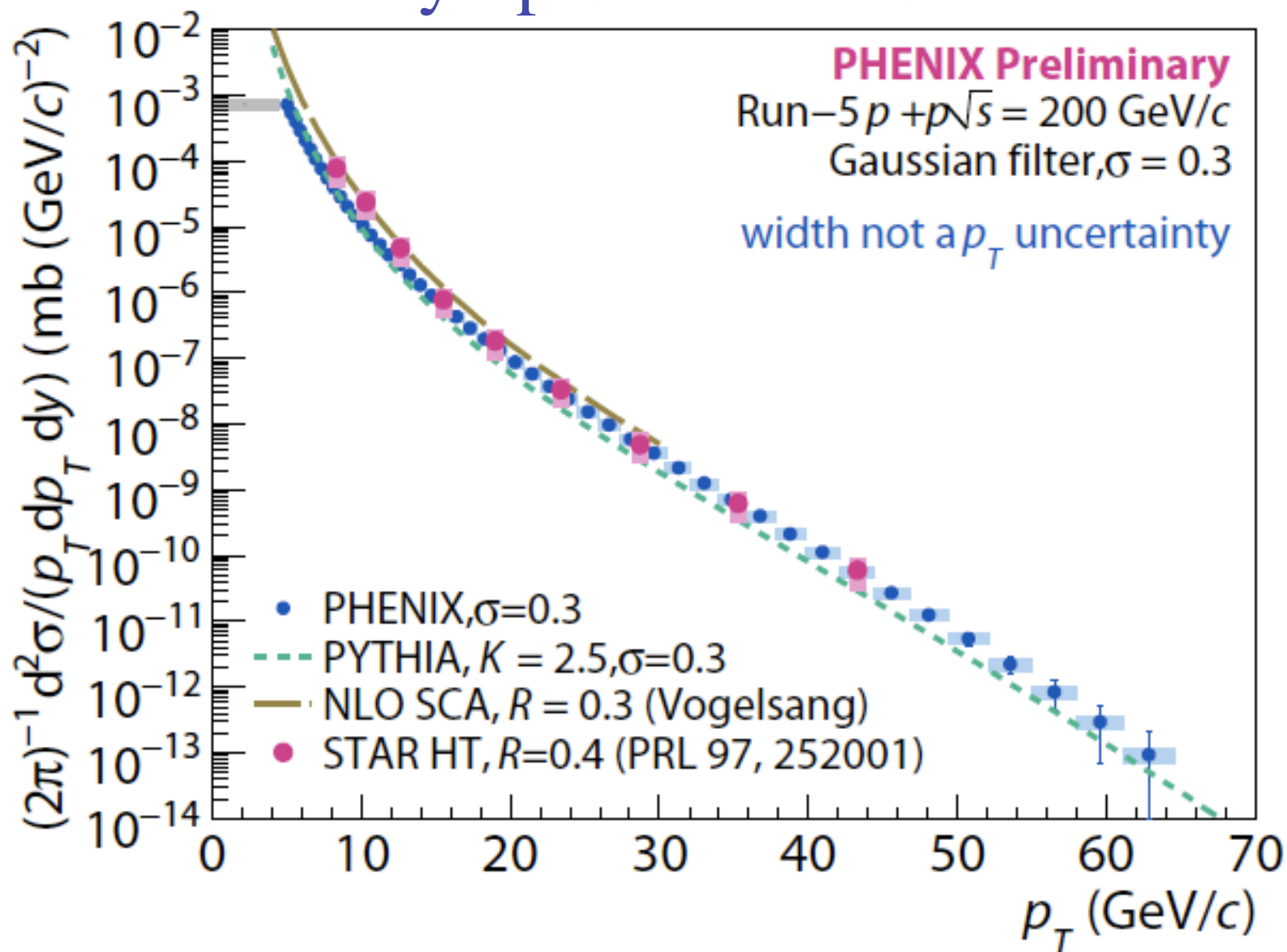
number
of colors

number
of flavors

$$b = (11N_c - 2N_f)/3$$

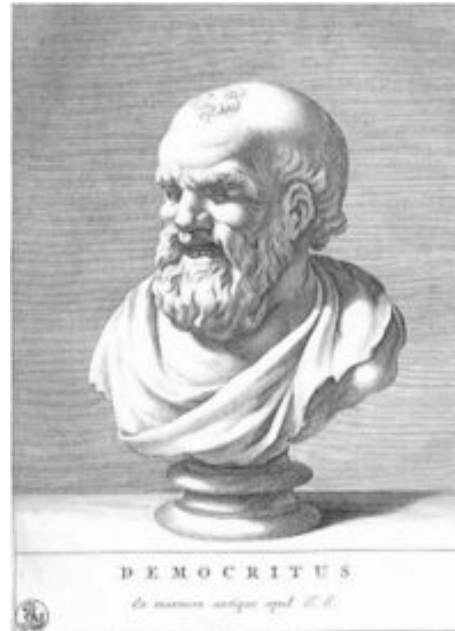
But: Strong confining interaction at large distances

Asymptotic Freedom



Where do we stand? (V B.C.)

- ❑ “Atoms”
- ❑ Geometry
- ❑ Void



Where do we stand? (2010 A.D.)

- ☒ “Atoms” identified: quarks and leptons
- ☐ Geometry (gauge field dynamics)
- ☐ Void (the structure of the vacuum)

The next step:
from particles (“atoms”) to fields (geometry)

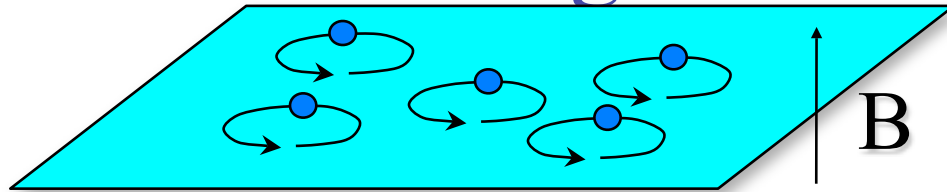
QCD: understanding the dynamics of gauge fields (geometry)

Problem

Measurements at RHIC

<input type="checkbox"/> Weak/vacuum fields	\longleftrightarrow	<input type="checkbox"/> Spin, parton fragmentation
<input type="checkbox"/> Strong static fields	\longleftrightarrow	<input type="checkbox"/> Small x distributions in nuclei
<input type="checkbox"/> Real-time dynamics	\longleftrightarrow	<input type="checkbox"/> EM probes, jets, heavy quarks
<input type="checkbox"/> Gauge fields with boundary conditions/ event horizons	\longleftrightarrow	<input type="checkbox"/> Bulk behavior, soft photons and dileptons
<input type="checkbox"/> Low-energy effective Theory of Everything: hydrodynamics	\longleftrightarrow	<input type="checkbox"/> Transport properties: shear and bulk viscosities, vorticity
<input type="checkbox"/> Topology of gauge fields	\longleftrightarrow	<input type="checkbox"/> Local parity violation, spin

Asymptotic freedom and strong color fields

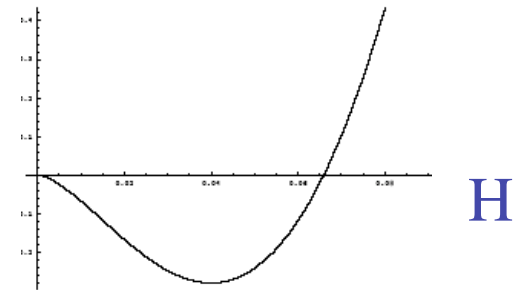


The effective potential: sum over 2D Landau levels

$$V_{\text{pert}}(H) = \frac{g H}{4 \pi^2} \int dp_z \sum_{n=0}^{\infty} \sum_{s_z=\pm 1} \sqrt{2 g H (n + 1/2 - s_z) + p_z^2}.$$

Paramagnetic response of the vacuum: V

$$\text{Re } V_{\text{pert}}(H) = \frac{1}{2} H^2 + (g H)^2 \frac{b}{32 \pi^2} \left(\ln \frac{g H}{\mu^2} - \frac{1}{2} \right)$$



1. The lowest level $n=0$ of radius $\sim (gH)^{-1/2}$ is **unstable!**

2. Strong fields \longleftrightarrow Short distances

Instability of perturbative QCD vacuum;
What is the true ground state?

QCD and the classical gauge fields

Classical dynamics applies when the action $S = \int d^4x \mathcal{L}(x)$ is large in units of the Planck constant (Bohr-Sommerfeld quantization)

$$\frac{S_{QCD}}{\hbar} \sim \frac{1}{g^2 \hbar} \int d^4x \operatorname{tr} G^{\mu\nu}(x) G_{\mu\nu}(x) \gg 1$$

(equivalent to setting $\hbar \rightarrow 0$)

=> Need weak coupling and strong fields

$$D_\mu = \partial_\mu - ig A_\mu^a t^a$$

$$A^2 \ll \frac{p^2}{g^2}$$

weak
field

$$A^2 \sim \frac{p^2}{g^2}$$

strong
field

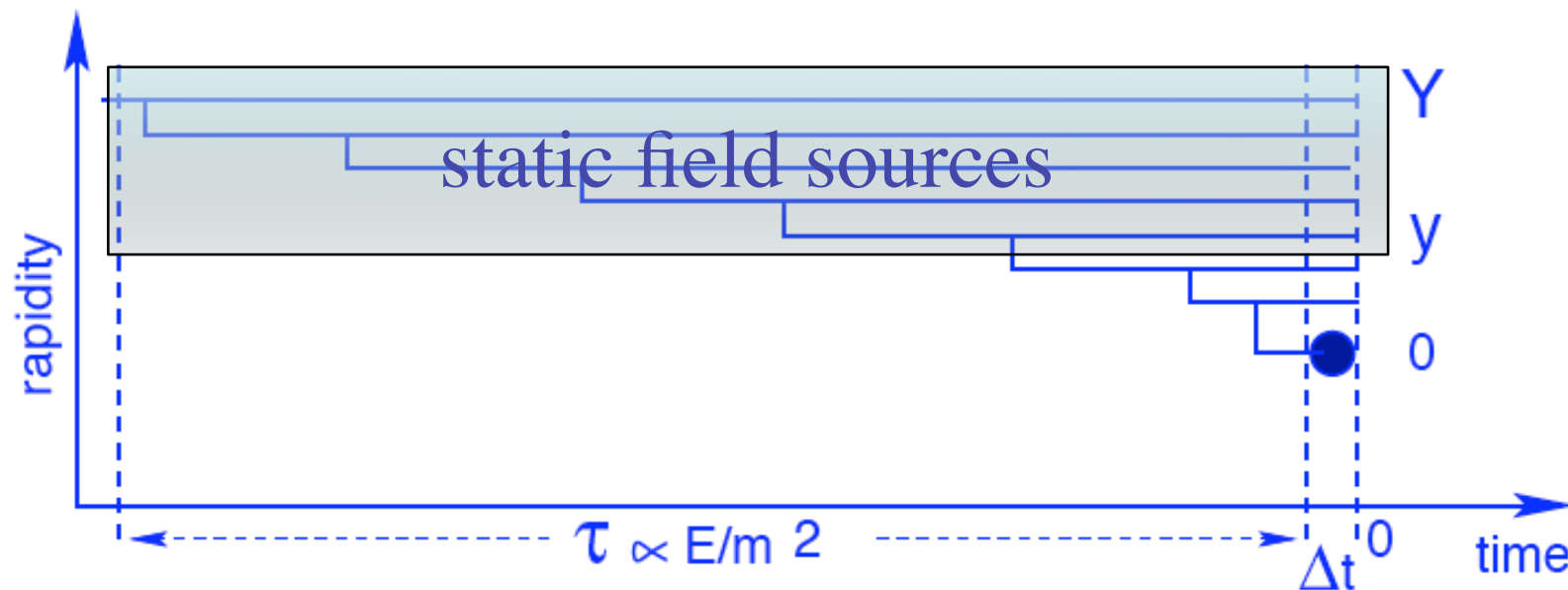
Weak coupling \neq perturbation theory!

The origin of classical background field

Measurements:

suppression of hard processes at forward y ;

depletion of back-to-back (quantum) correlations



Gluons with large rapidity and large occupation number
act as a background field for the production of slower gluons

“Color Glass Condensate”

Measuring the strength of evolving color fields

PHENIX Coll.,
arXiv:1005.1627

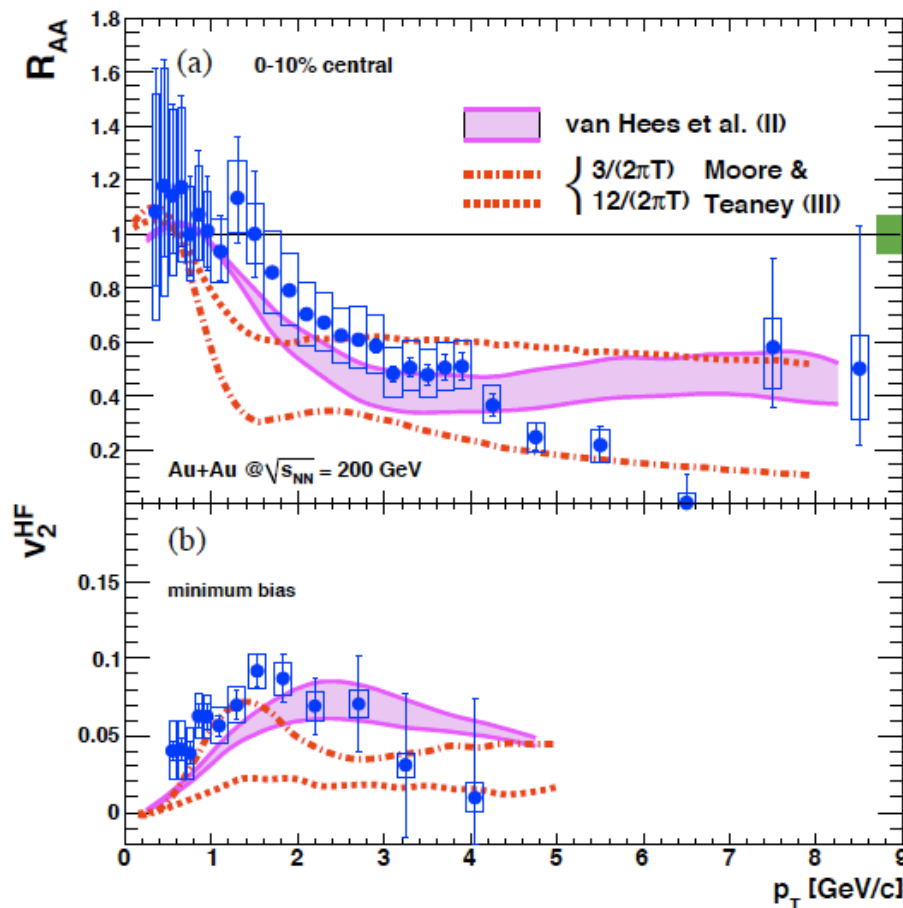


FIG. 40: (Color online) Comparison of Langevin-based models from [74–76] to the heavy flavor electron R_{AuAu} for 0–10% centrality and v_2 for minimum-bias collisions.

About the same
behavior of heavy
and light quarks -
the color field
is very strong,

$$F \sim m_c^2$$

may be weakly
coupled but
not perturbative

Measuring the strength of color fields

PHENIX Coll.,
arXiv:1005.1627

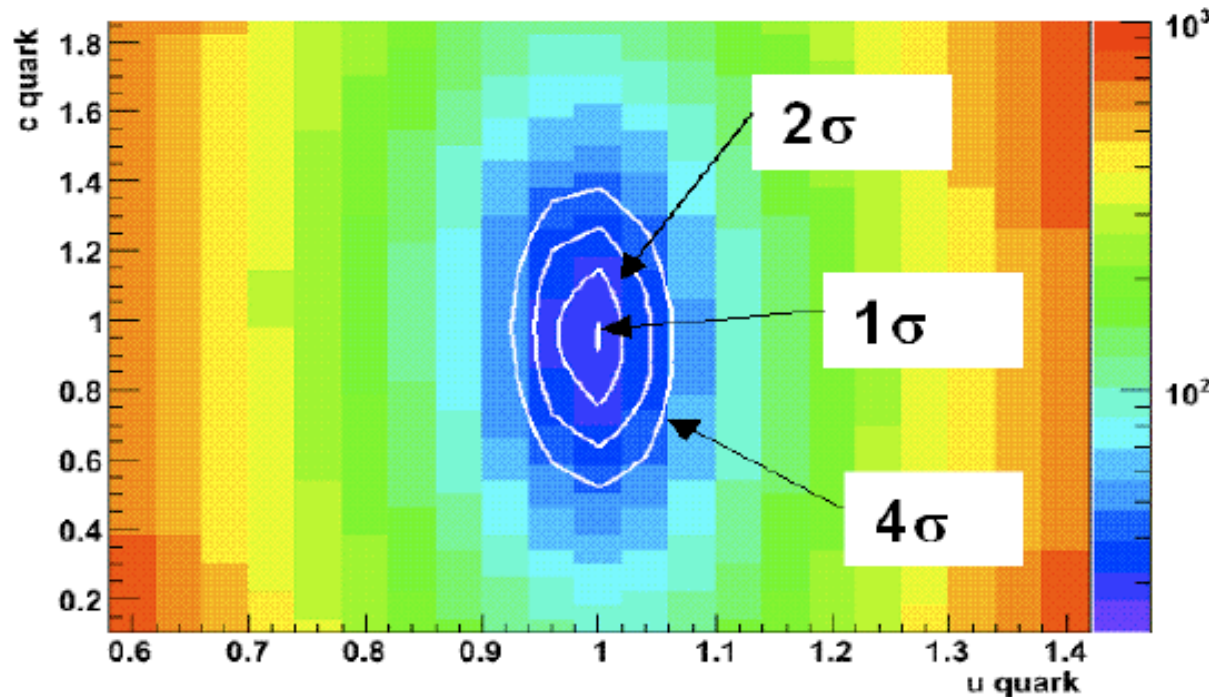


FIG. 46: (Color online) χ^2 map as a function of the light quark v_2 (horizontal axis) and charm quark v_2 (vertical axis), each divided by the measured light quark v_2 .

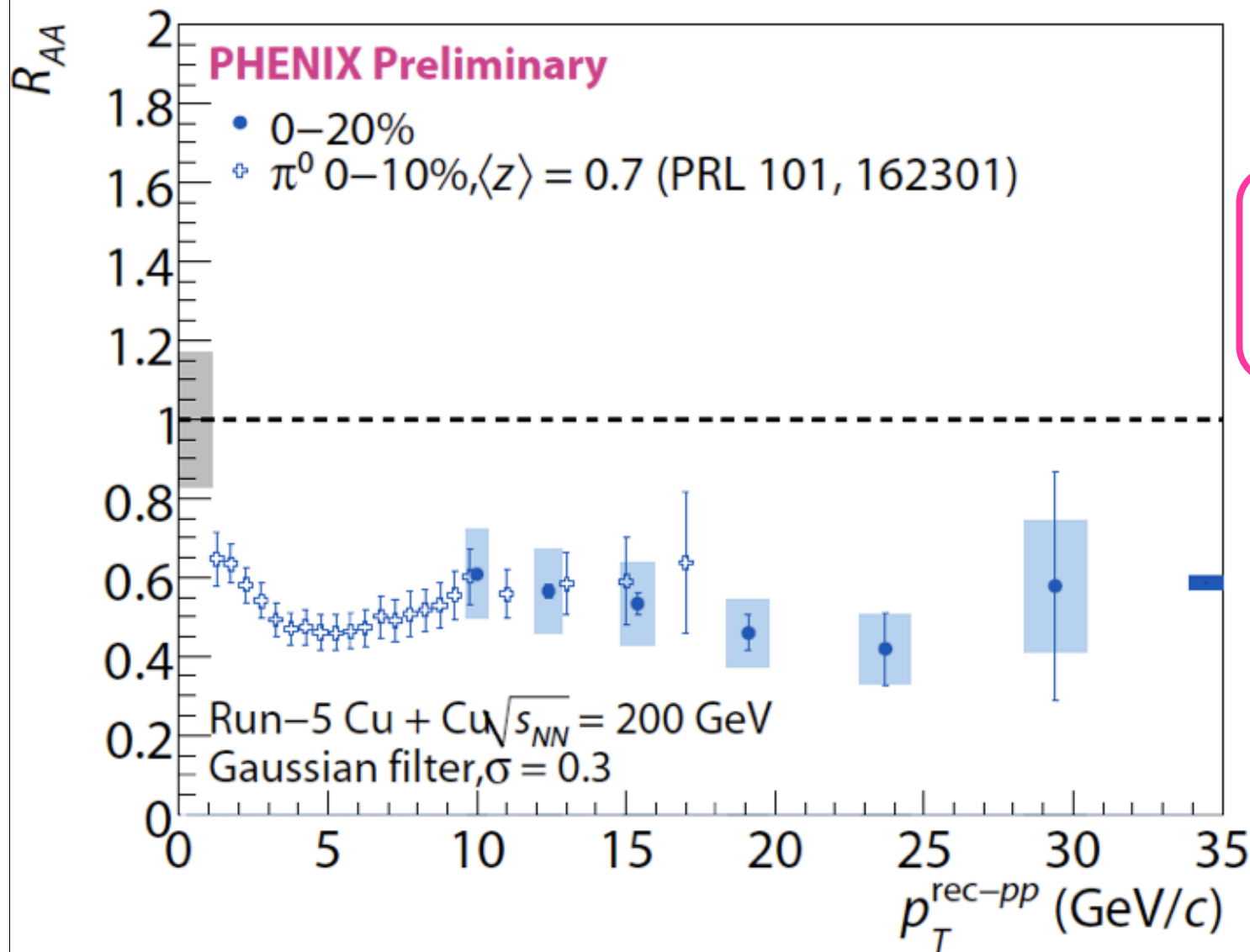
About the same behavior of heavy and light quarks - the color field is very strong,

$$F \sim m_c^2$$

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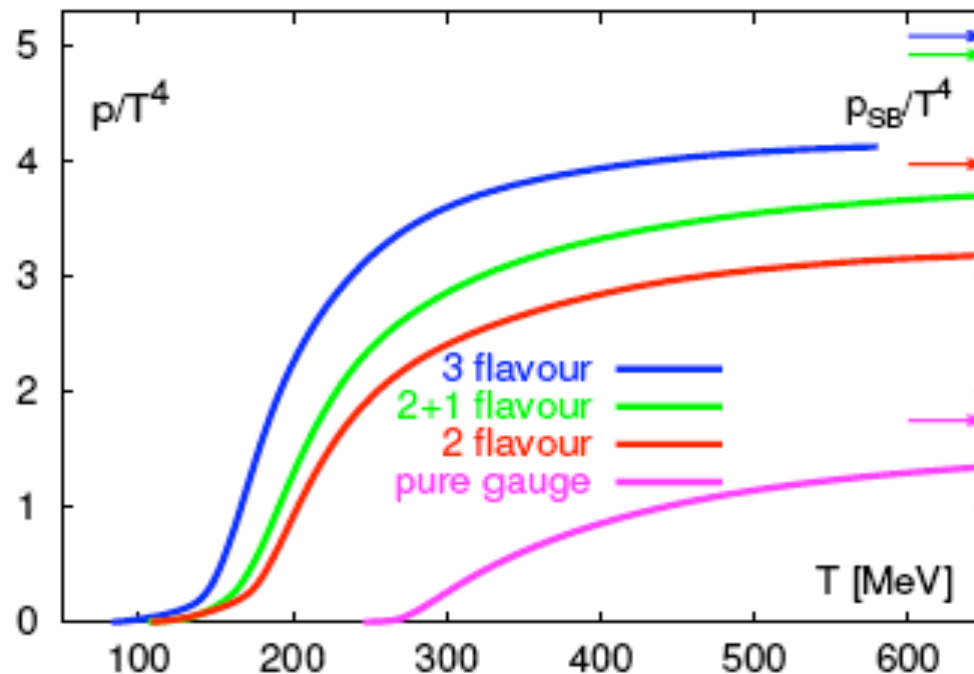
To calibrate the field strength, must separate b from c ¹⁹

Jets and leading hadrons: measuring the strength of color fields



Measurement:
modification of
jet shape?

QCD at high temperatures: gauge fields with boundary conditions



Phase transitions:

deconfinement

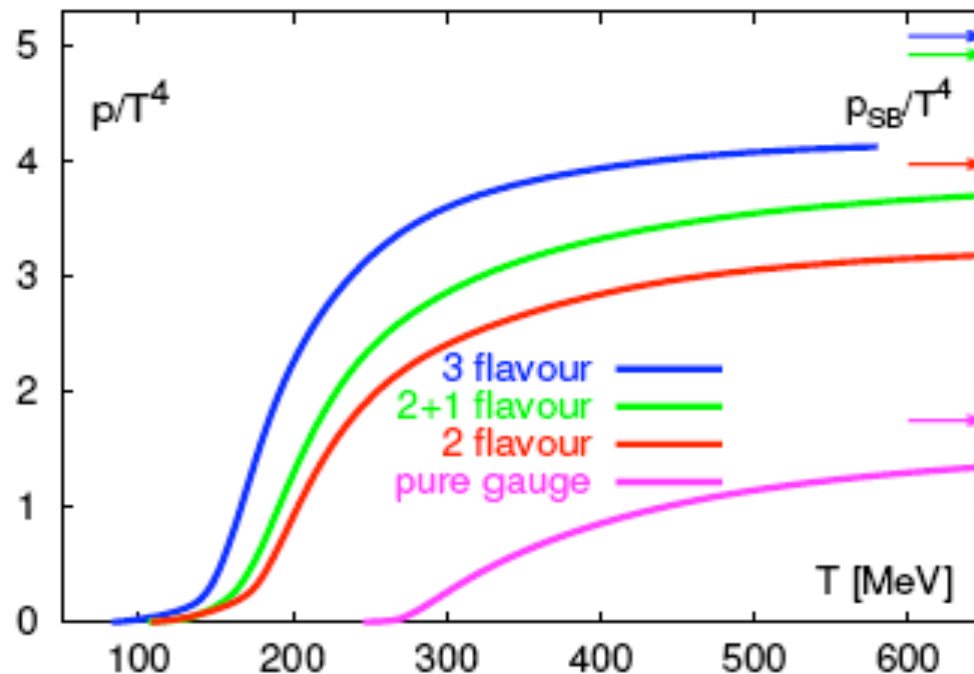
Chiral symmetry
restoration

$U_A(1)$ restoration

Data from lattice QCD simulations F. Karsch et al

**Is $T \sim 200$ MeV “hot” or “cold”? The answer depends
on the strength of interactions and gauge field dynamics**

QCD at high temperatures: gauge fields with boundary conditions



Phase transitions:

deconfinement

Chiral symmetry
restoration

$U_A(1)$ restoration

Data from lattice QCD simulations F. Karsch et al

**By convention hot, by convention cold,
but in reality atoms and void;**

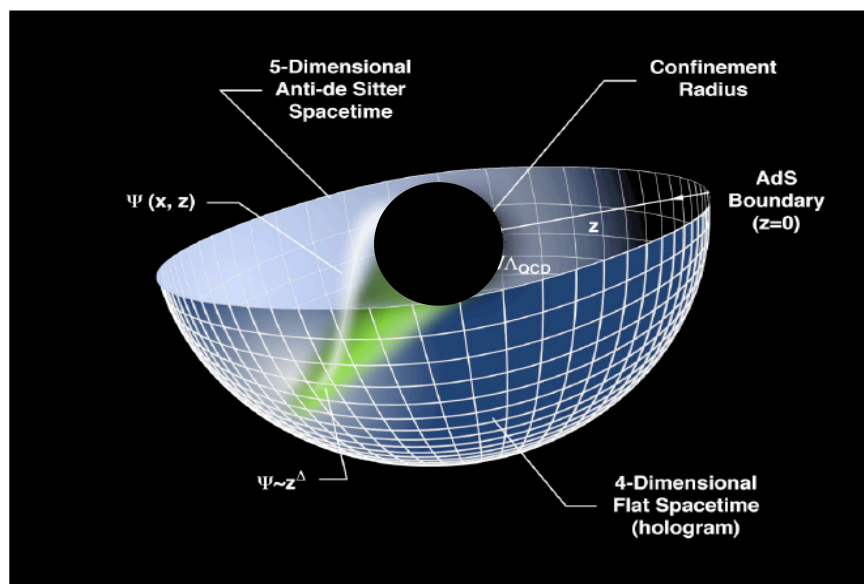
and also in reality we know nothing, since the truth is at bottom.

Democritus

Low-energy effective ToE: hydrodynamics

Holographic view:

Particle contents of
supergravity:
**gravitons, dilatons,
axions**



Caveman's view:

■ Shear viscosity

■ Bulk viscosity

■ Rate of topological
transitions

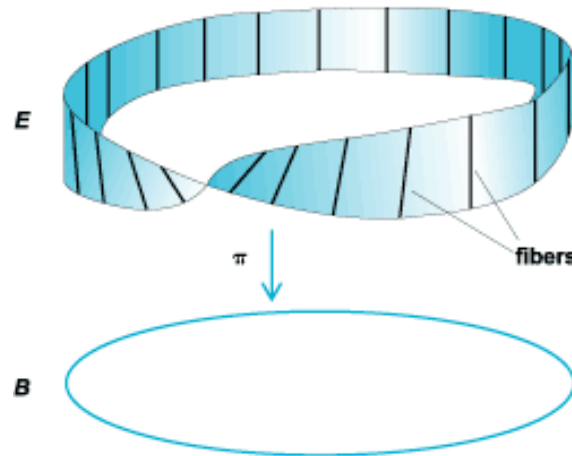
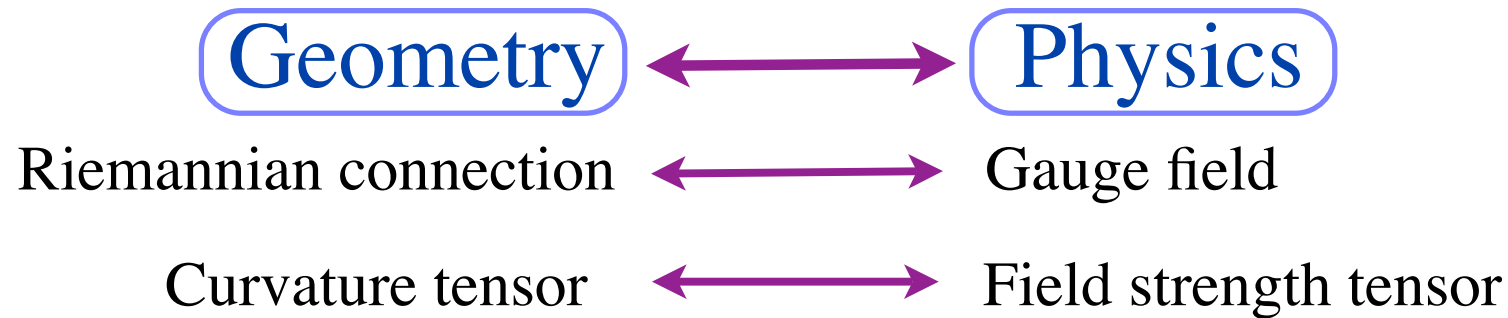
AdS₅ “Reality”:

■ Graviton propagation

■ Dilaton propagation

■ Axion propagation

Topology of gauge fields



Möbius strip, the simplest nontrivial example of a fiber bundle

Gauge theories “live” in a fiber bundle space that possesses non-trivial topology (knots, links, twists,...)

Topology of gauge fields: Chern-Simons forms

CHARACTERISTIC FORMS

$$(6.1) \quad TP_1(\theta) = \frac{1}{4\pi^2} \{ \theta_{12} \wedge \theta_{13} \wedge \theta_{23} + \theta_{12} \wedge \Omega_{12} + \theta_{13} \wedge \Omega_{13} + \theta_{23} \wedge \Omega_{23} \} .$$

What does it mean for a gauge theory?

Geometry



Physics

Riemannian connection



Gauge field

Curvature tensor



Field strength tensor

$$S_{CS} = \frac{k}{8\pi} \int_M d^3x \, \epsilon^{ijk} \left(A_i F_{jk} + \frac{2}{3} A_i [A_j, A_k] \right)$$

 **breaks Parity invariance**

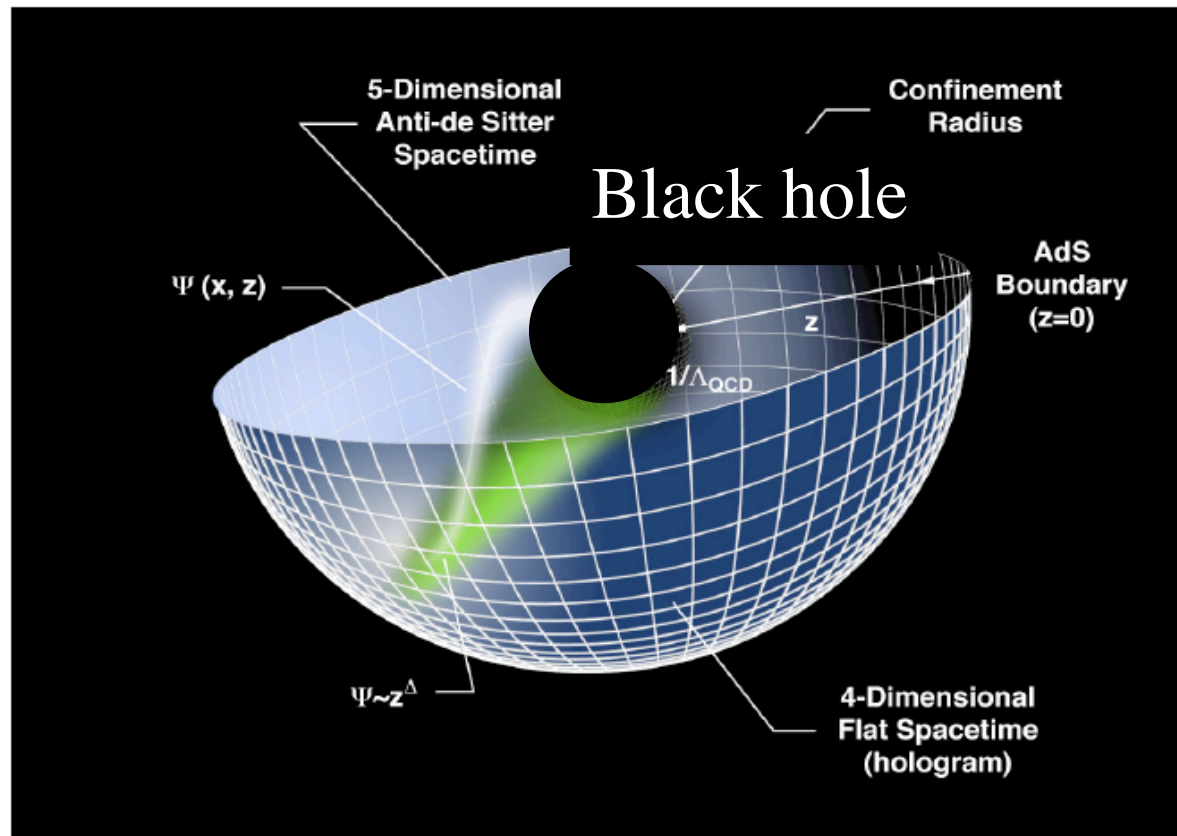
Abelian non-Abelian
(magnetic helicity)

Topology at strong coupling: holographic view

Chern-Simons number
diffusion rate
at strong coupling

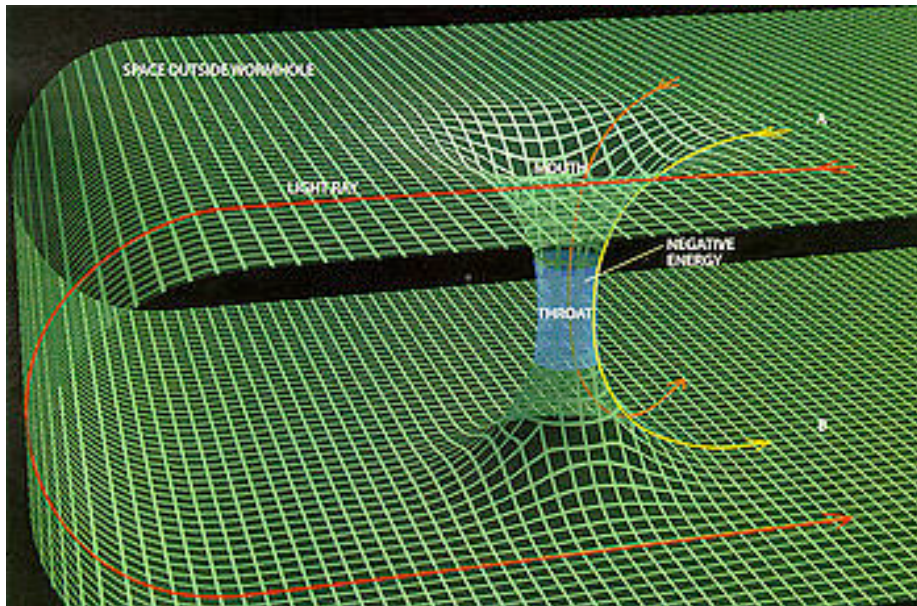
$$\Gamma = \frac{(g_{\text{YM}}^2 N)^2}{256\pi^3} T^4$$

D.Son,
A.Starinets
hep-th/
020505



NB: This calculation is completely analogous to the calculation of shear viscosity: **“perfect liquid”** contains strong topological fluctuations

Topology at strong coupling: holographic view



D-instanton as
an Einstein-Rosen
wormhole;
the flow of RR charge
down the throat of
the wormhole describes
change of chirality

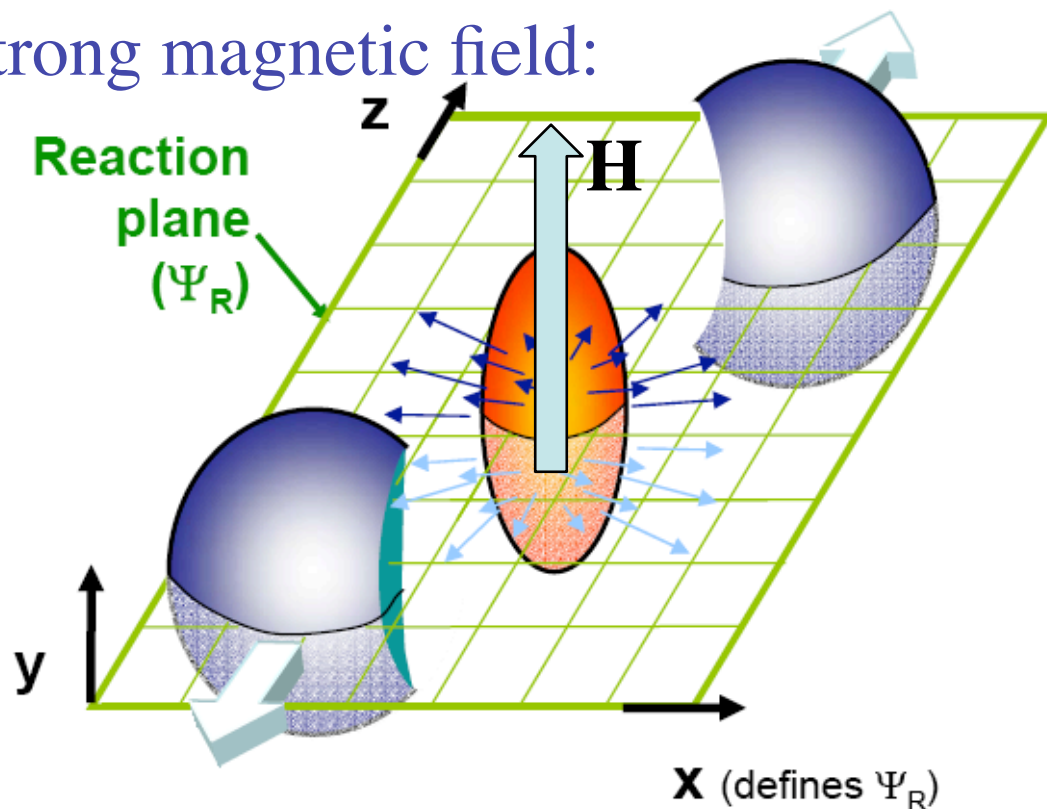
G. W. Gibbons, M. B. Green and M. J. Perry, Phys. Lett. B **370**, 37
(1996) [arXiv:hep-th/9511080].

D-instantons as a source of multiparticle production in N=4 SYM?

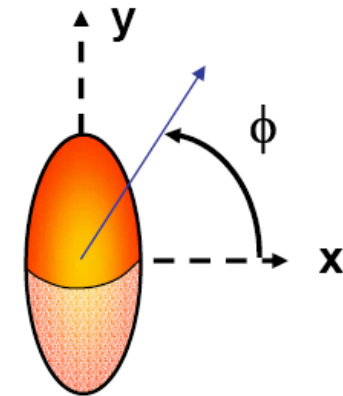
DK, E. Levin, arXiv:0910.3355

Is there a way to observe topological charge fluctuations in experiment?

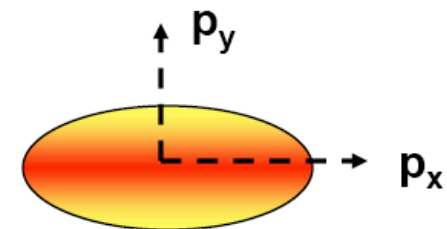
Relativistic ions create
a strong magnetic field:



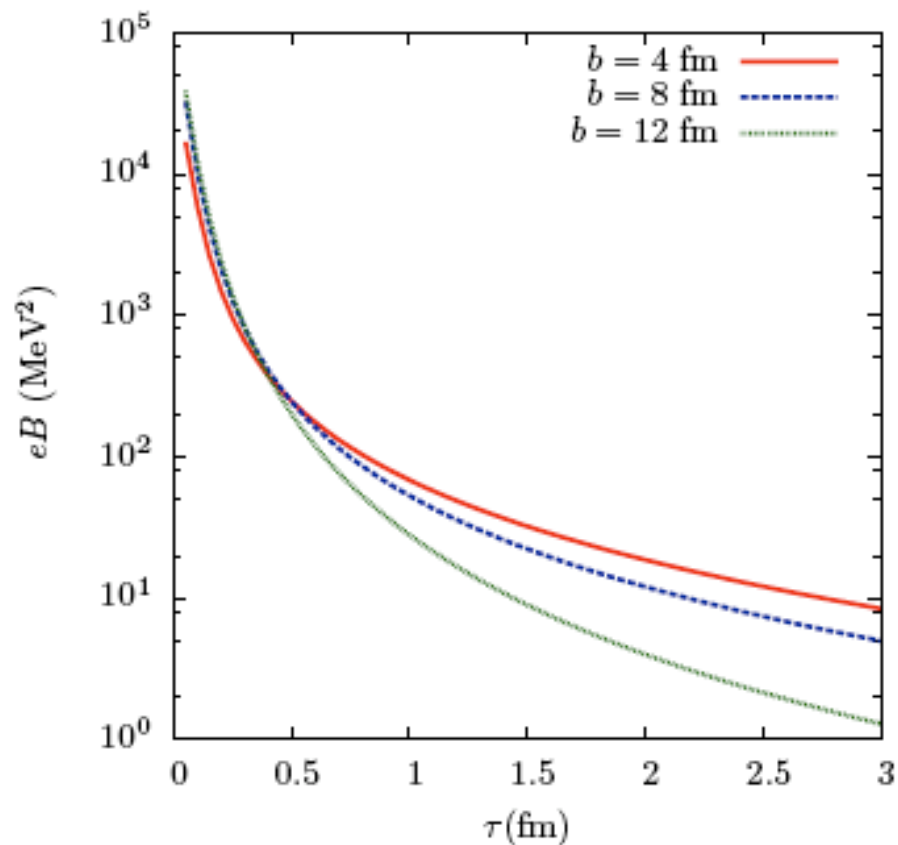
Initial spatial anisotropy



Final momentum anisotropy



Heavy ion collisions as a source of the strongest magnetic fields available in the Laboratory



In a conducting plasma, Faraday induction can make the field long-lived:

K.Tuchin, arXiv:1006.3051

Vorticity! Develop MHD of QCD fluid

DK, McLerran, Warringa, Nucl Phys A803(2008)227

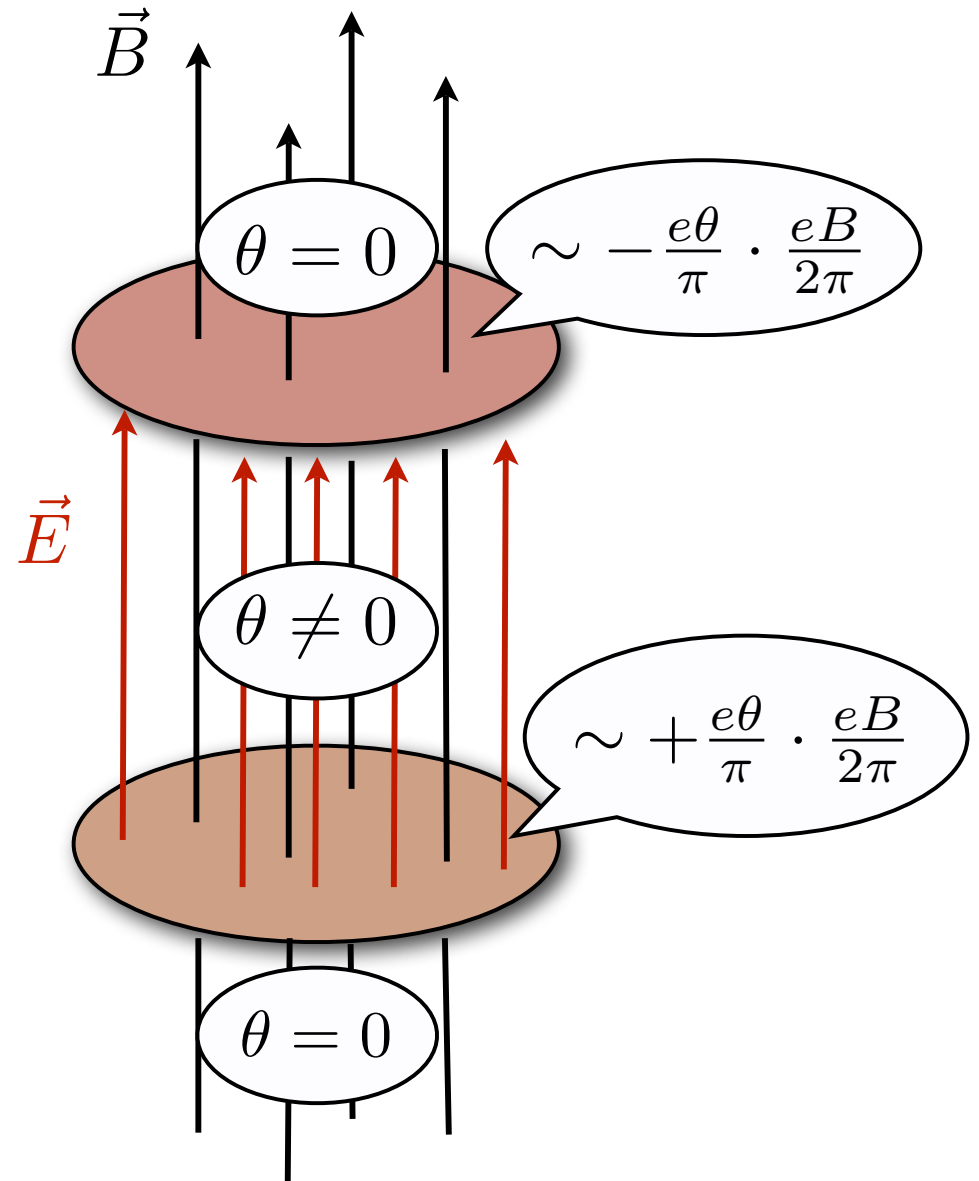
Fig. A.2. Magnetic field at the center of a gold-gold collision, for different impact parameters. Here the center of mass energy is 200 GeV per nucleon pair ($Y_0 = 5.4$).

The Chiral Magnetic Effect

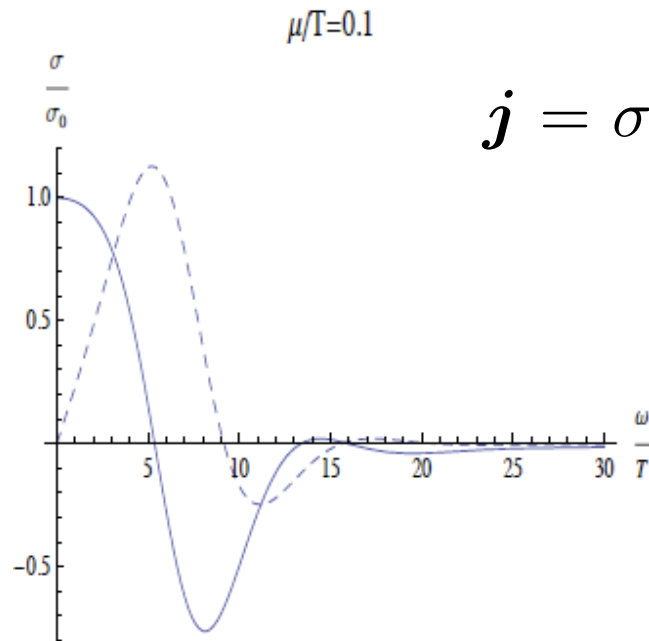
$$\vec{\nabla} \cdot \vec{E} = \rho + c\vec{P} \cdot \vec{B}$$

$$\vec{P} \equiv \vec{\nabla} \theta$$

$$d_e = \sum_f q_f^2 \left(e \frac{\theta}{\pi} \right) \left(\frac{eB \cdot S}{2\pi} \right) L$$



Holographic CME: is the current renormalized at strong coupling?



$$\mathbf{j} = \sigma_{\chi} \mathbf{B}$$

Recent progress:

V. Rubakov, arXiv:1005.1888;

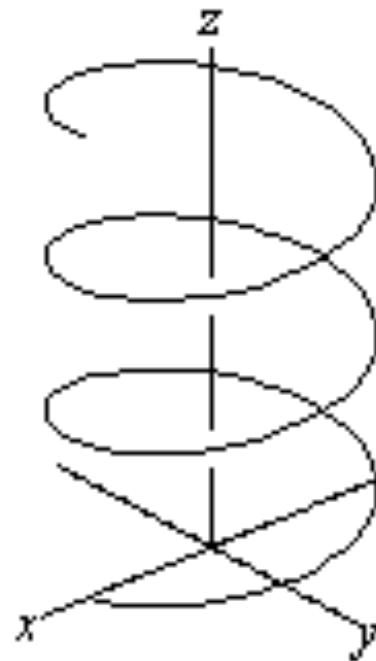
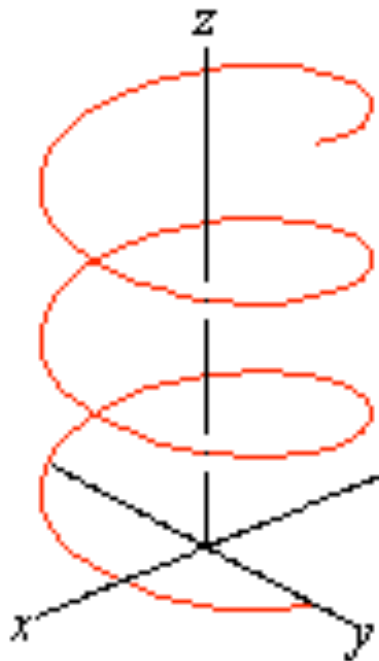
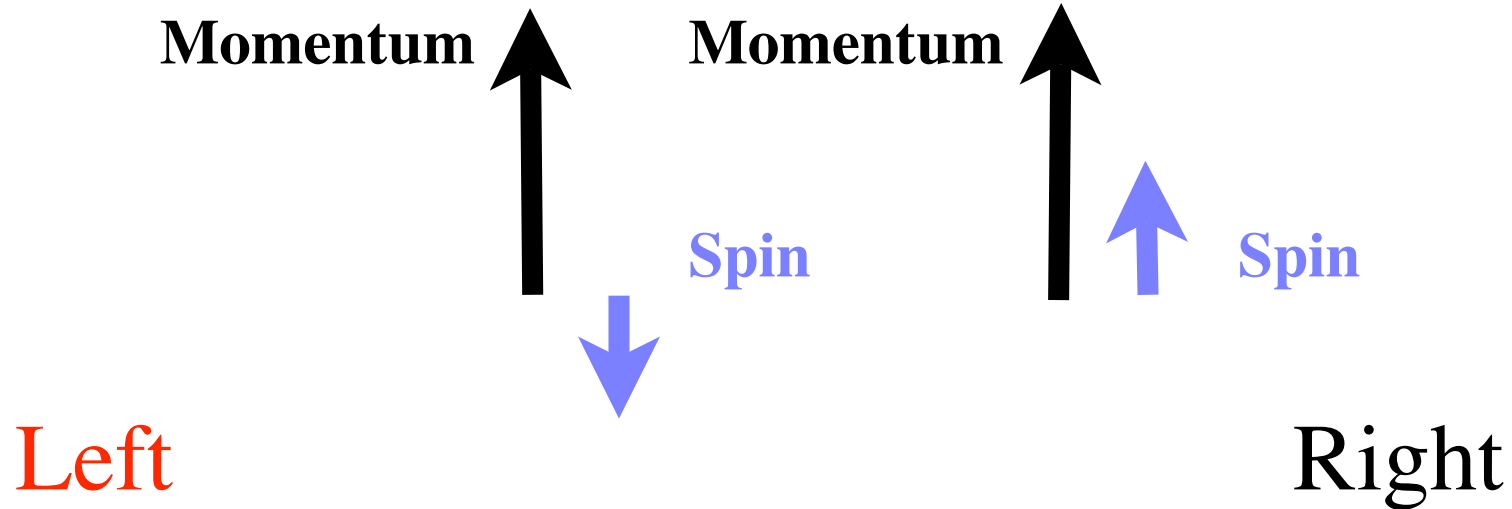
A. Gynther, K. Landsteiner, F. Pena-Benitez, A. Rebhan,
arXiv:1005.2587

**CME current is the same at
strong and weak coupling**

H.-U. Yee, arXiv:0908.4189,
JHEP 0911:085, 2009

What carries the current
at strong coupling?

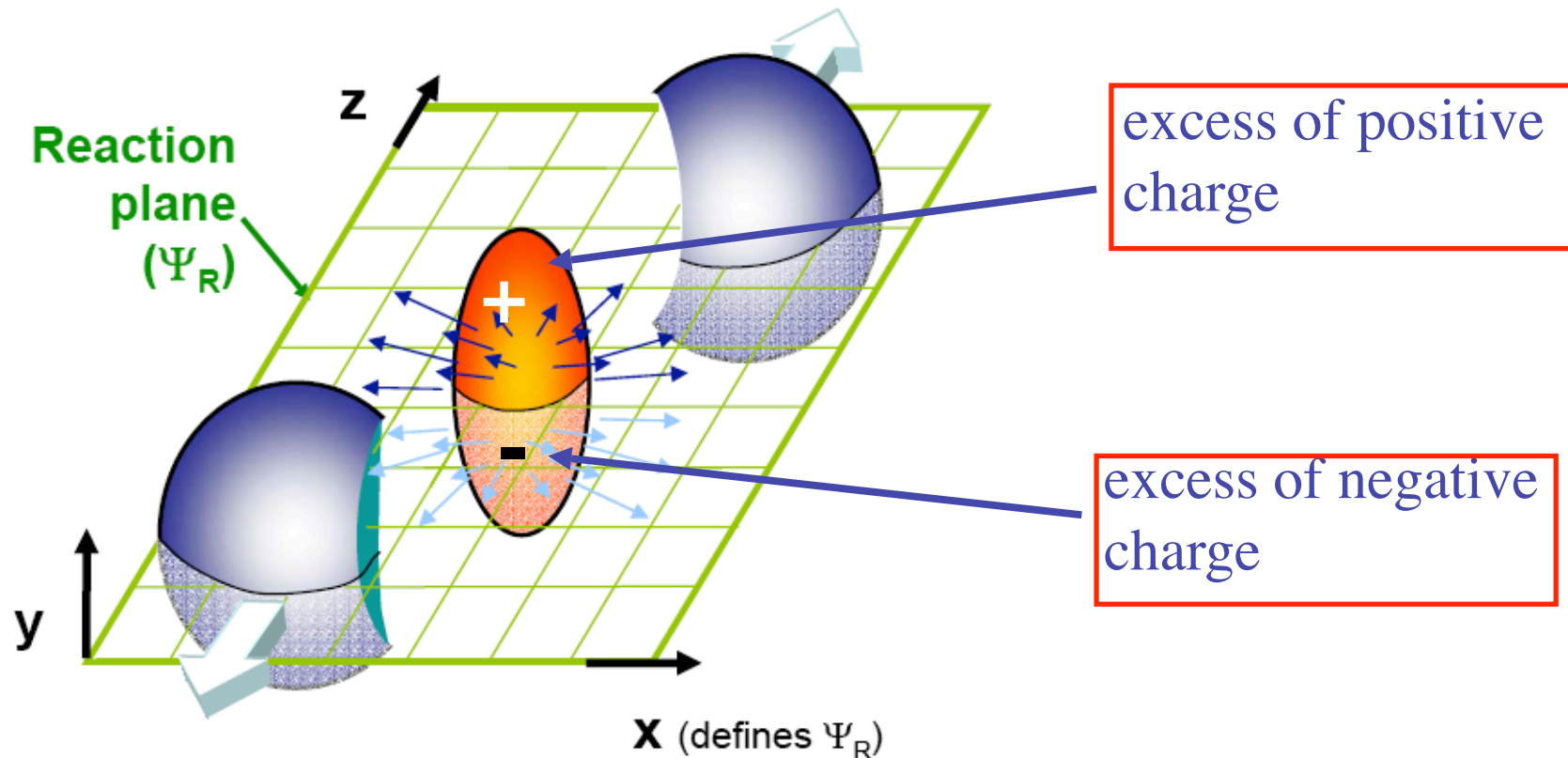
CME in the chirally broken phase





“Quark-gluon
solenoid”,
Physics,
June 18, 2010

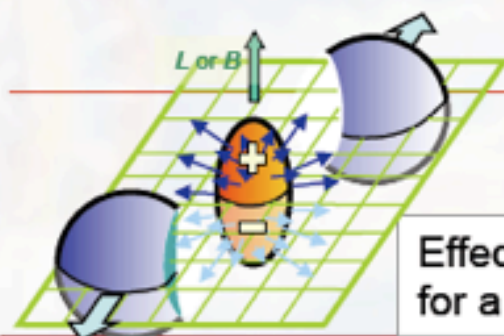
Charge asymmetry w.r.t. reaction plane as a signature of local strong P violation



Electric dipole moment of QCD matter!

Observable

S.A. Voloshin, Phys. Rev. C 70 (2004) 057901

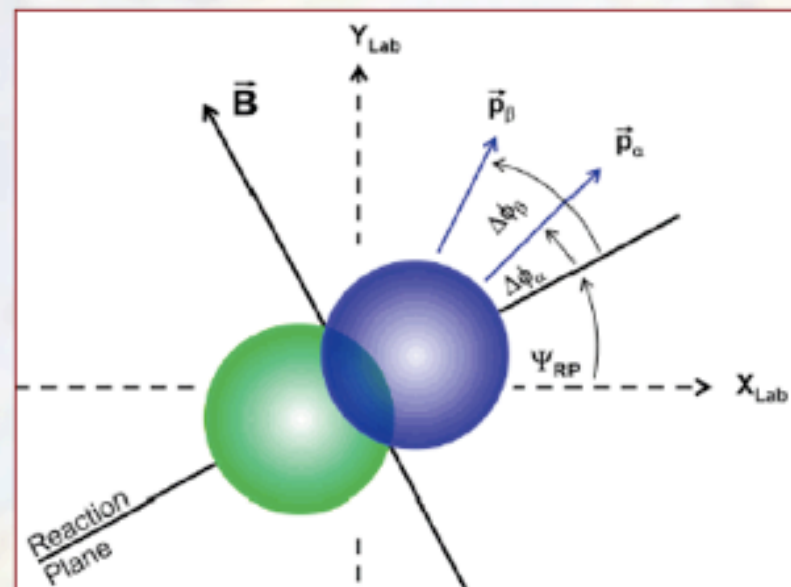


Effective particle distribution for a certain Q .

$$\frac{dN_\alpha}{d\phi} \propto 1 + 2v_{1,\alpha} \cos(\Delta\phi) + 2v_{2,\alpha} \cos(2\Delta\phi) + \dots \\ + 2a_{1,\alpha} \sin(\Delta\phi) + 2a_{2,\alpha} \sin(2\Delta\phi) + \dots,$$

$$\Delta\phi = (\phi - \Psi_{RP})$$

- The effect is too small to observe in a single event
- The sign of Q varies and $\langle a \rangle = 0$ (we consider only the leading, first harmonic) \rightarrow one has to measure correlations, $\langle a_\alpha a_\beta \rangle$, **\mathcal{P} -even quantity (!)**
- $\langle a_\alpha a_\beta \rangle$ is expected to be $\sim 10^{-4}$
- $\langle a_\alpha a_\beta \rangle$ can not be measured as $\langle \sin \phi_\alpha \sin \phi_\beta \rangle$ due to large contribution from effects not related to the orientation of the reaction plane
- \rightarrow study the difference in corr's in- and out-of-plane



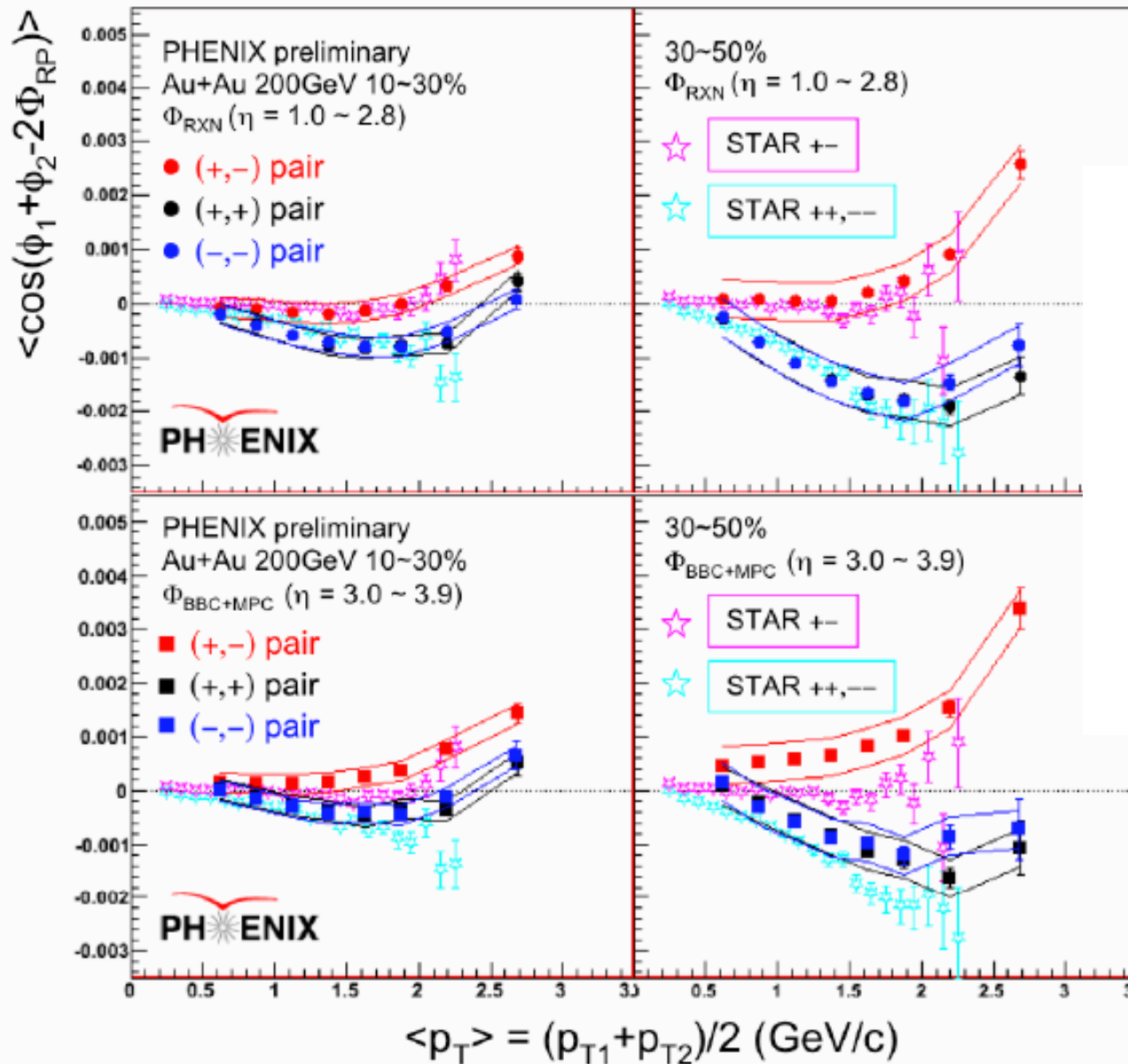
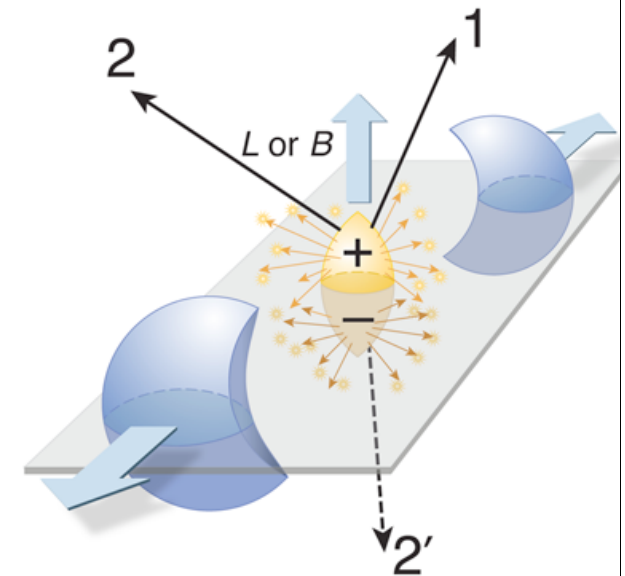
$$\langle \cos(\phi_\alpha + \phi_\beta - 2\Psi_{RP}) \rangle = \\ = \langle \cos \Delta\phi_\alpha \cos \Delta\phi_\beta \rangle - \langle \sin \Delta\phi_\alpha \sin \Delta\phi_\beta \rangle \\ = [\langle v_{1,\alpha} v_{1,\beta} \rangle + B^{in}] - [\langle a_\alpha a_\beta \rangle + B^{out}].$$

$$B^{in} \approx B^{out}, \quad v_1 = 0$$

A practical approach: three particle correlations:

$$\langle \cos(\phi_\alpha + \phi_\beta - 2\phi_c) \rangle = \langle \cos(\phi_\alpha + \phi_\beta - 2\Psi_{RP}) \rangle v_{2,c}$$

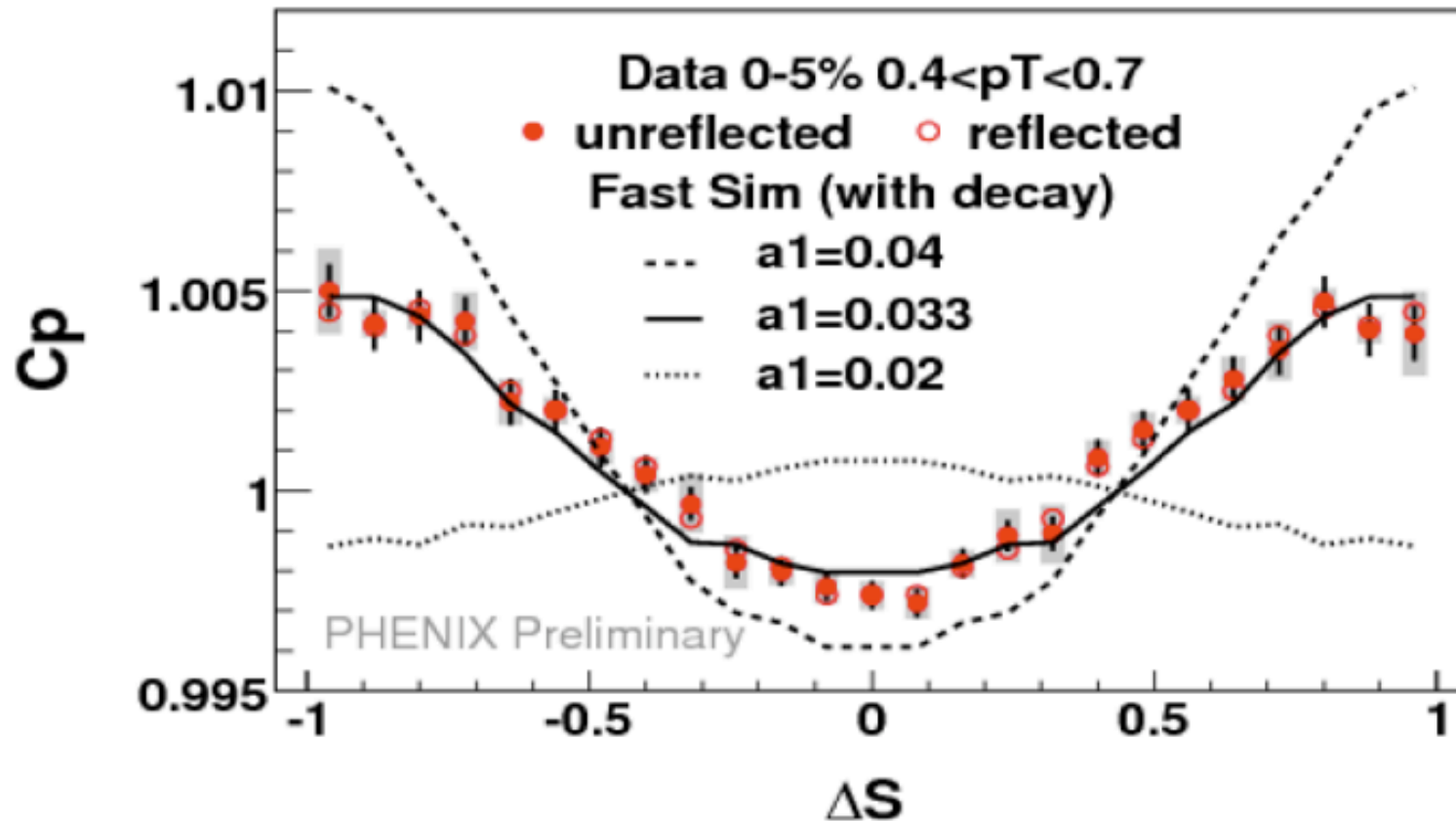
S.Esumi et al
[PHENIX Coll]
April 2010



R. Lacey
[PHENIX Coll]
Talk at “CP-odd”,
April 26-30, 2010

Relatively good agreement between PHENIX & STAR

Multi-particle correlation Results



Concave shape validates charge asymmetry w.r.t the reaction plane

N. Ajitanand [PHENIX Coll], Talk @ BNL, Dec 2009

Are the observed fluctuations of charge asymmetries a convincing evidence for the local parity violation?

A number of open questions that still have to be clarified:

in-plane vs out-of-plane,
new observables?

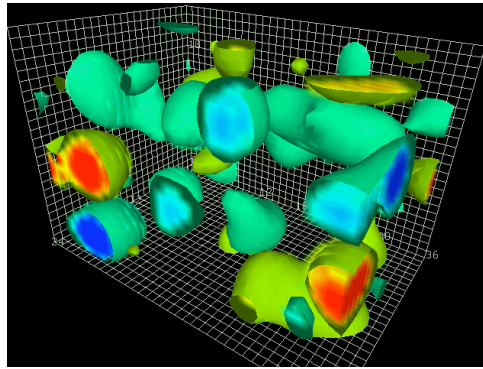
A. Bzdak, V. Koch, J. Liao,
arXiv:0912.5050; 1005.5380

physics “backgrounds”

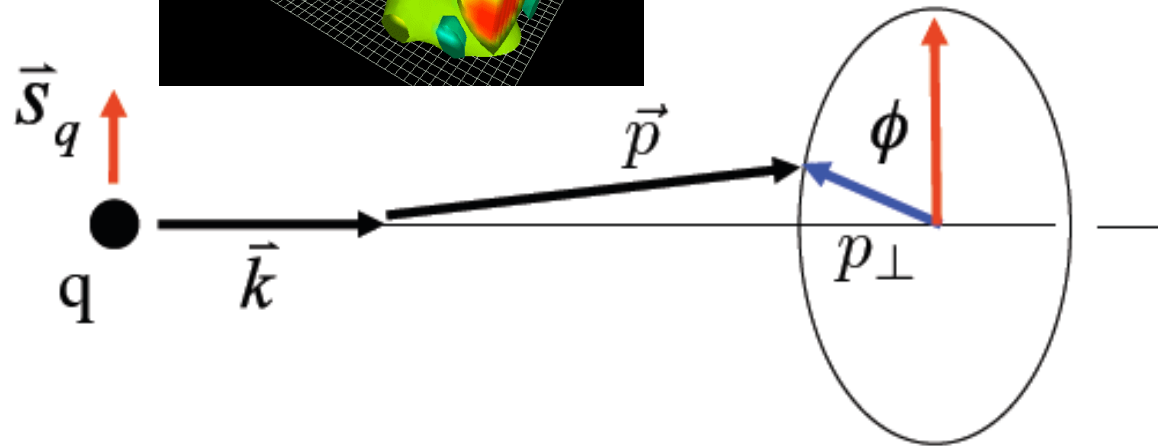
M. Asakawa, A. Majumder, B. Muller,
arXiv:1003.2436
S. Pratt and S. Schlichting, arXiv:1005.5341
F. Wang, arXiv: 0911.1482

Fortunately, a number of analytical and numerical (lattice)
tools are available to theorists,
and the new data (low energy, **PID asymmetries**, U-U)
will hopefully come - this question can be answered! ³⁸

Topology of gauge fields, LPV, and the fragmentation of polarized quarks



Z. Kang, DK, arXiv:1006.2132



P-odd:

$$D_{\pi/q\uparrow}(z, p_{\perp}) = D(z, p_{\perp}^2) + H_1^{\perp}(z, p_{\perp}^2) \frac{(\hat{k} \times p_{\perp}) \cdot s_q}{M} + \tilde{H}_1^{\perp}(z, p_{\perp}^2) \frac{p_{\perp} \cdot s_q}{M}$$

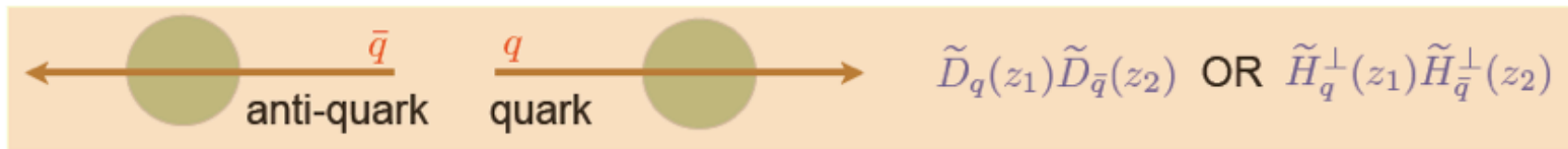
Cross section in e+e- annihilation:

Data and tests (Belle, RHIC) forthcoming:
M.Grosse-Perdekamp, A. Vossen,
A. Deshpande, ...

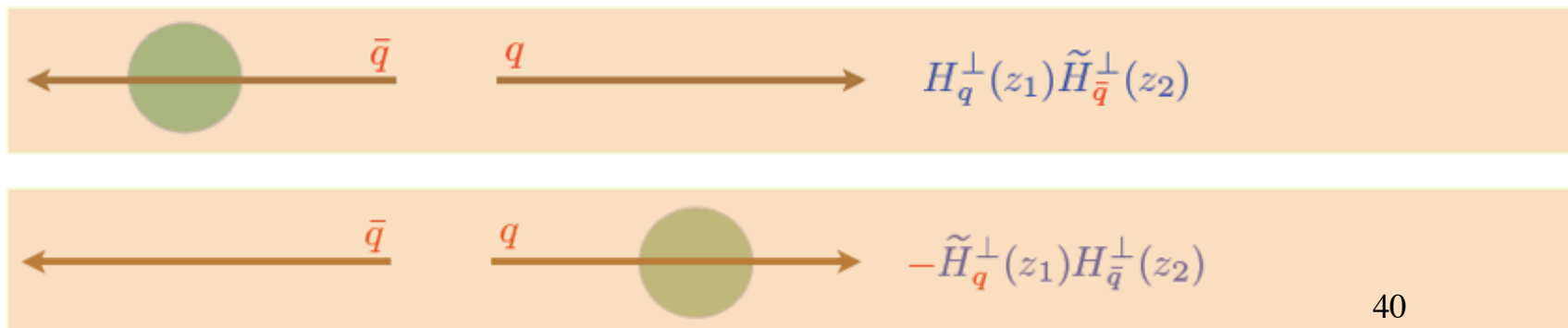
$$\frac{d\sigma}{dz_1 dz_2 d\cos\theta d(\phi_1 + \phi_2)} = \sigma_0 \sum_q e_q^2 \left\{ (1 + \cos^2\theta) \left[D_q(z_1) D_{\bar{q}}(z_2) - \tilde{D}_q(z_1) \tilde{D}_{\bar{q}}(z_2) \right] \right. \\ \left. + \sin^2\theta \cos(\phi_1 + \phi_2) \left[H_q^\perp(z_1) H_{\bar{q}}^\perp(z_2) + \tilde{H}_q^\perp(z_1) \tilde{H}_{\bar{q}}^\perp(z_2) \right] \right. \\ \left. + \sin^2\theta \sin(\phi_1 + \phi_2) \left[H_q^\perp(z_1) \tilde{H}_{\bar{q}}^\perp(z_2) - \tilde{H}_q^\perp(z_1) H_{\bar{q}}^\perp(z_2) \right] \right\} \quad \begin{array}{l} \text{“Collins} \\ \text{effect”} \\ \text{P-odd,} \\ \text{only} \\ \text{EbyE} \end{array}$$

Physical pictures:

P-odd times P-odd terms:



P-odd term alone:



Summary

The next decade presents us with a unique chance to pursue the centuries-old quest for understanding the structure of matter

- ☒ “Atoms” identified: quarks and leptons
- ☐ Geometry (gauge field dynamics)
- ☐ Void (the structure of the vacuum)

The next step:
from particles (“atoms”) to fields (geometry)

QCD: understanding the dynamics of gauge fields (geometry)

Problem

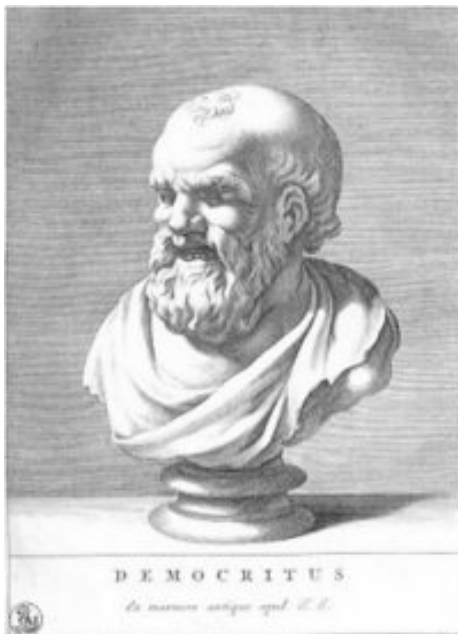
Measurements at RHIC

<input type="checkbox"/> Weak/vacuum fields	\longleftrightarrow	<input type="checkbox"/> Spin, parton fragmentation
<input type="checkbox"/> Strong static fields	\longleftrightarrow	<input type="checkbox"/> Small x distributions in nuclei
<input type="checkbox"/> Real-time dynamics	\longleftrightarrow	<input type="checkbox"/> EM probes, jets, heavy quarks
<input type="checkbox"/> Gauge fields with boundary conditions/ event horizons	\longleftrightarrow	<input type="checkbox"/> Bulk behavior, soft photons and dileptons
<input type="checkbox"/> Low-energy effective Theory of Everything: hydrodynamics	\longleftrightarrow	<input type="checkbox"/> Transport properties: shear and bulk viscosities, vorticity
<input type="checkbox"/> Topology of gauge fields	\longleftrightarrow	<input type="checkbox"/> Local parity violation, spin

Extra slides



Leucippus, V B.C.



Democritus, ca 460 -370 B.C.

Atomism vs corpuscularianism:

are quarks and leptons
the ultimate indivisible
“atoms” of Nature?

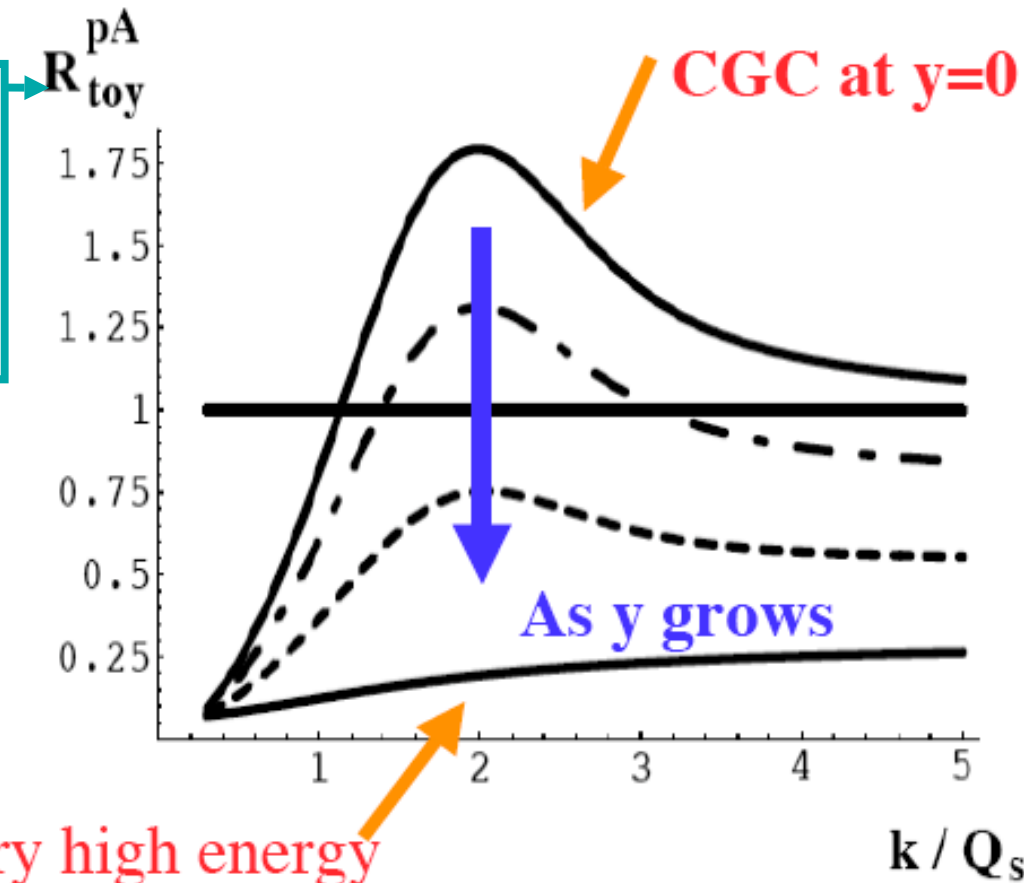


Robert Boyle (1627–1691)

Page from alchemic treatise of
[Ramon Llull](#), 16th century

Static strong color fields: nuclear gluon distributions at small x

The ratio
of pA and
pp cross
sections



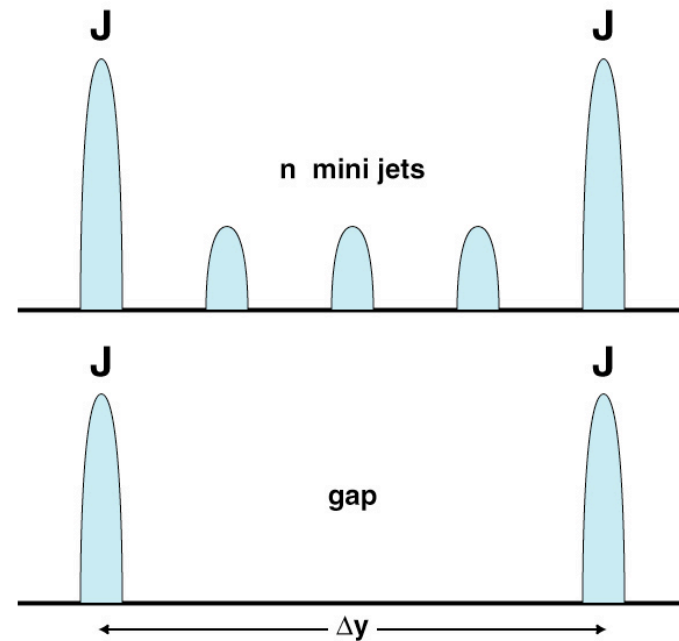
transverse
momentum

At large rapidity y (small angle) expect
suppression of hard particles!

DK, Levin, McLerran;
Albacete, Armesto, Kovner,
Wiedemann; DK, Kovchegov,
Tuchin⁴⁵

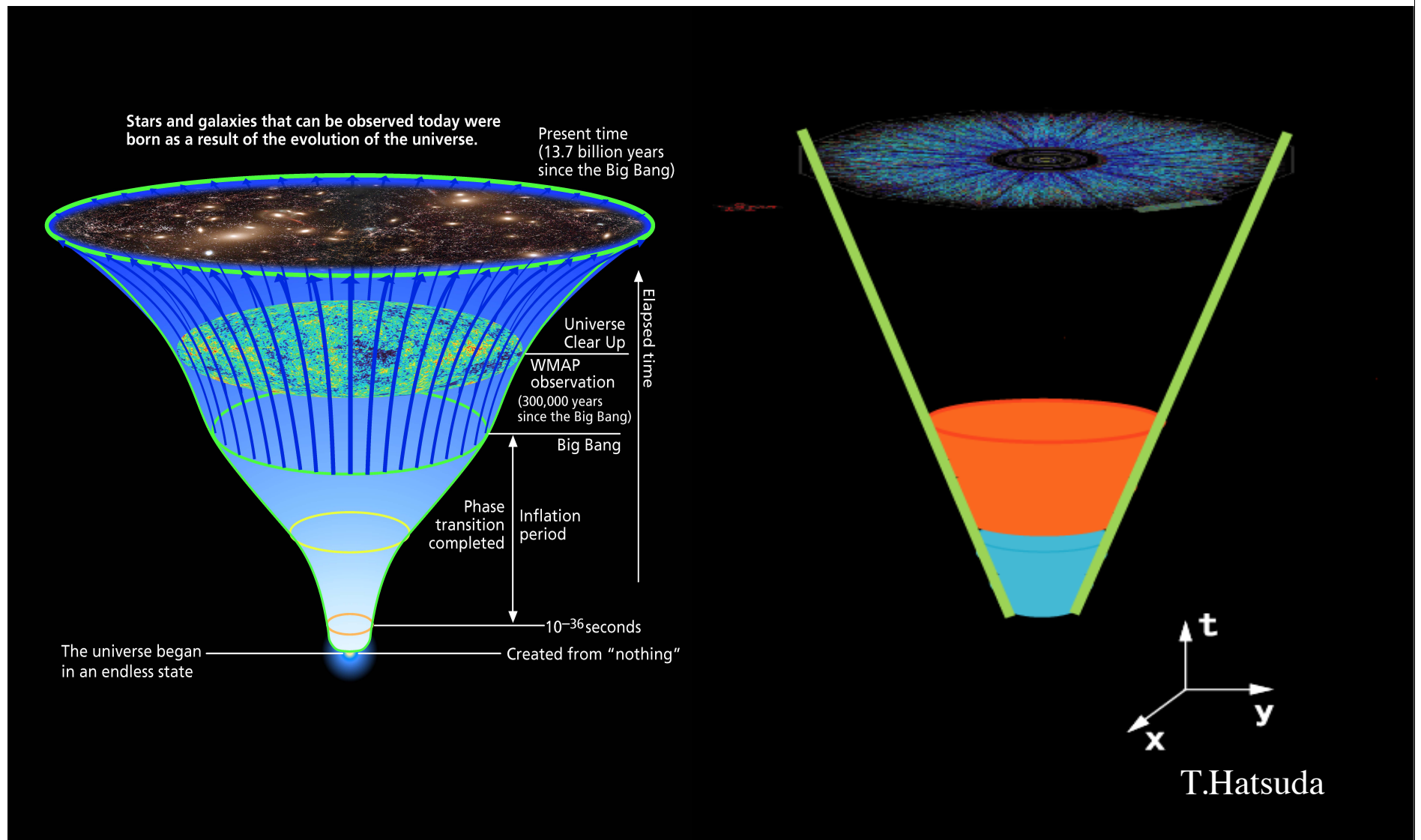
Are the effects observed at forward rapidity due to parton saturation in the CGC?

- Back-to-back correlations for jets separated by several units of rapidity are very sensitive to the evolution effects (“Mueller-Navelet jets”) and to the presence of CGC

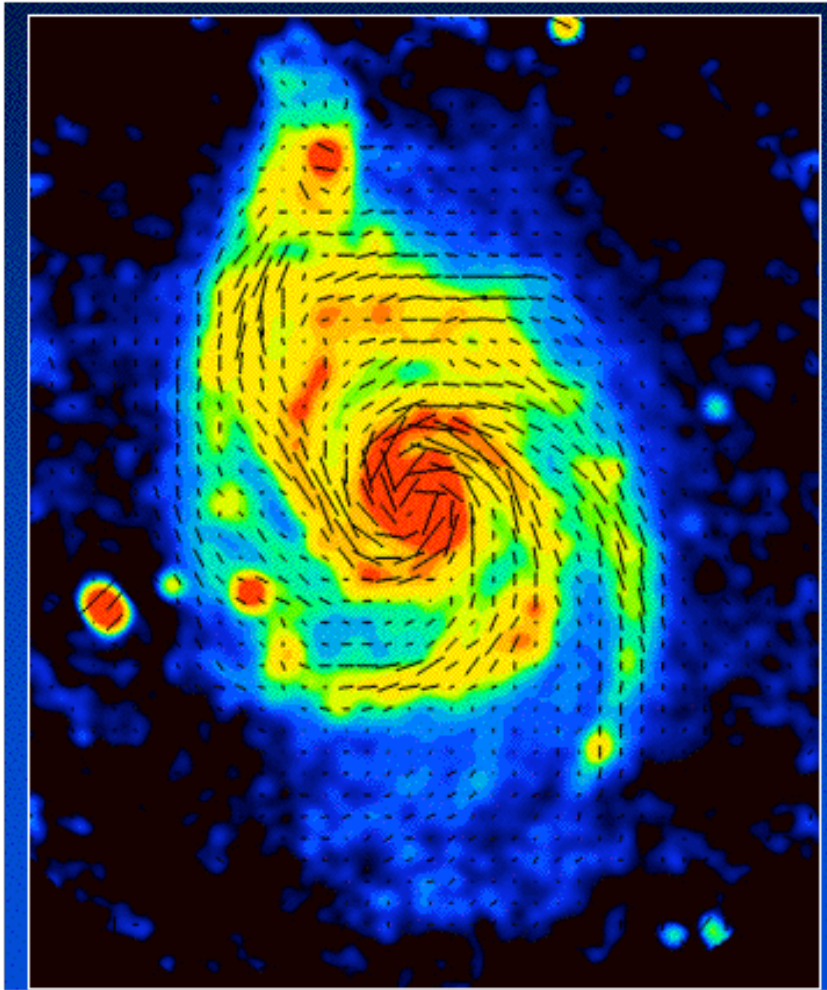


Forward measurements at RHIC:
Do back-to-back correlations really disappear?

Topology in the Early Universe?



What is the origin of cosmic magnetic helicity?



Magnetic fields are abundant in the Universe at large scales:

3 μG field in Milky Way;

1-40 μG fields in clusters of galaxies

Is the entire Universe chiral?

e.g. M.Longo, arXiv:0812.3437;
thanks to J.Bjorken

Magnetic field in M51:
Polarization of emission
Beck 2000

Chiral magnetic spiral in the Early Universe?

Affleck-Dine baryogenesis

